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VALENCE LANGUAGES GENERATED BY EQUALITY SETS

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ABSTRACT

We consider the generalized equality set, i.e., the set of solutions of the generalized Post Correspondence Problem. Actually we study the solutions of a special instances where one of the morphisms is periodic and the begin word is a letter. We considering the languages defined by mapping the equality set by a coding, and prove that the family achieved is exactly family of regular valence languages over \mathbb{Z} .

 $Keywords\colon$ Regular valence grammar, morphism, equality sets, Post Correspondence Problem

1. Introduction

Valence grammars were introduced by Păun in [11]. In general, in these grammars the productions are associated an integer value, and the generated language consists of those words that have a derivation the valences of which add up to zero. It is rather easy to show that the family of regular valence languages equals the family of languages recognized by integer weighted finite automata, see [4, 5]. This family of languages is also equal to the family of languages recognized by blind counter automata as defined by Greibach in [3].

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